

# Model Predictive Control for Smart Energy Systems

**John Bagterp Jørgensen**  
Technical University of Denmark

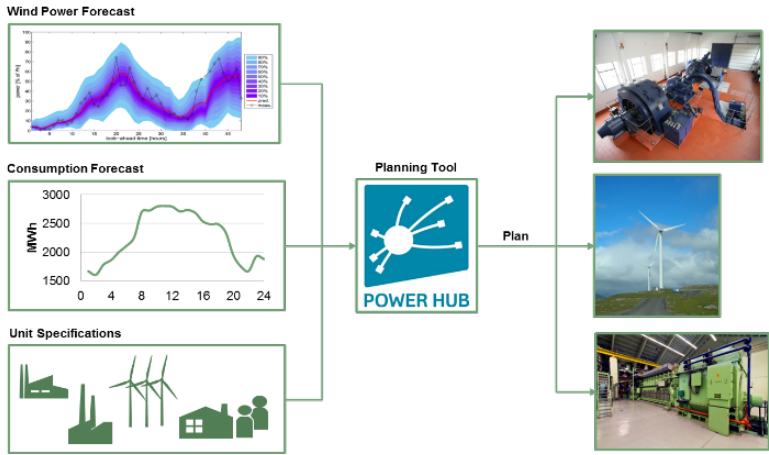
Energiråd Ringkøbing-Skjern  
September 11, 2020  
Ringkøbing, Denmark

# Digitalization, Control and Optimization of Smart Coordinated Energy Systems





# Optimization based control = Model Predictive Control (MPC)



$$\frac{\partial C_i}{\partial a} = -v_i \frac{\partial C_i}{\partial z} + D \frac{\partial^2 C_i}{\partial z^2} + \frac{k}{\epsilon_i} (C_i - C_i)$$

$$\frac{\partial C_c}{\partial a} = -v_c \frac{\partial C_c}{\partial z} + D \frac{\partial^2 C_c}{\partial z^2} + \frac{k}{\epsilon_c} (C_i - C_c) + \gamma r_c$$

$$\frac{\partial W_{reg}}{\partial a} = -v_c \frac{\partial W_{reg}}{\partial z} + D \frac{\partial^2 W_{reg}}{\partial z^2} + r_c$$

$$\frac{\partial T_i}{\partial a} = -v_i \frac{\partial T_i}{\partial z} + D \frac{\partial^2 T_i}{\partial z^2} + \frac{h}{\epsilon_i} (T_i - T_i)$$

$$\frac{\partial T_c}{\partial a} = -v_c \frac{\partial T_c}{\partial z} + D \frac{\partial^2 T_c}{\partial z^2} + \frac{h}{\epsilon_c} (T_i - T_c) - \Delta H_i r_c$$

**Powerful  
Computers**

$$\min_x \quad x^T Q x + c^T x$$

$$\text{s.t.} \quad A_{ieq} x \leq b_{ieq}$$

$$A_{eq} x = b_{eq}$$

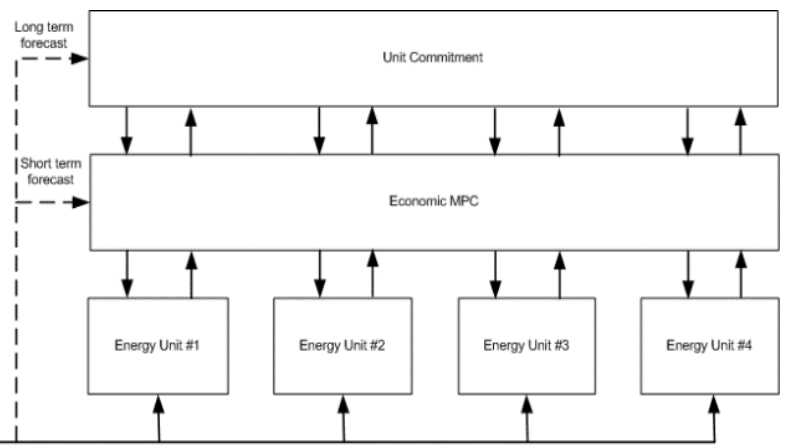
$$l \leq x \leq u$$

$$x_i x_j = 0 \quad \forall (i, j) \in \Phi$$

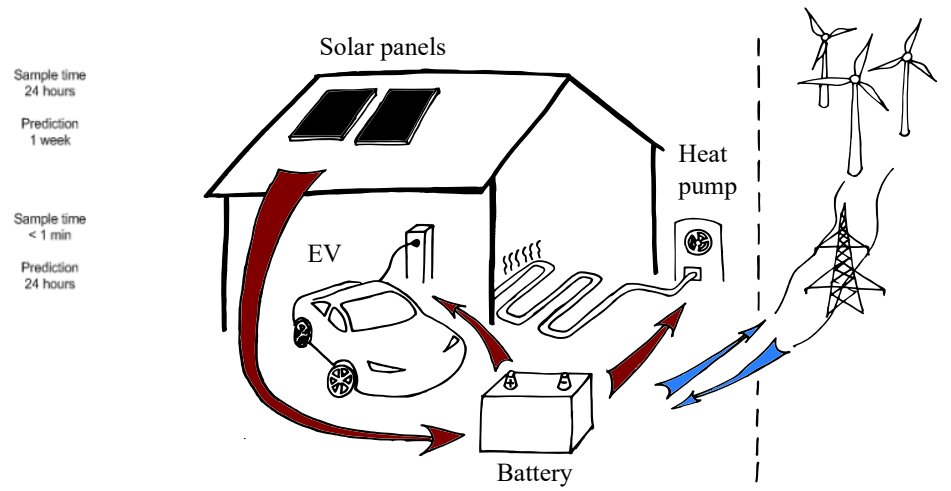
**Mathematical / Statistical  
Modelling**

**Optimization  
Algorithms**

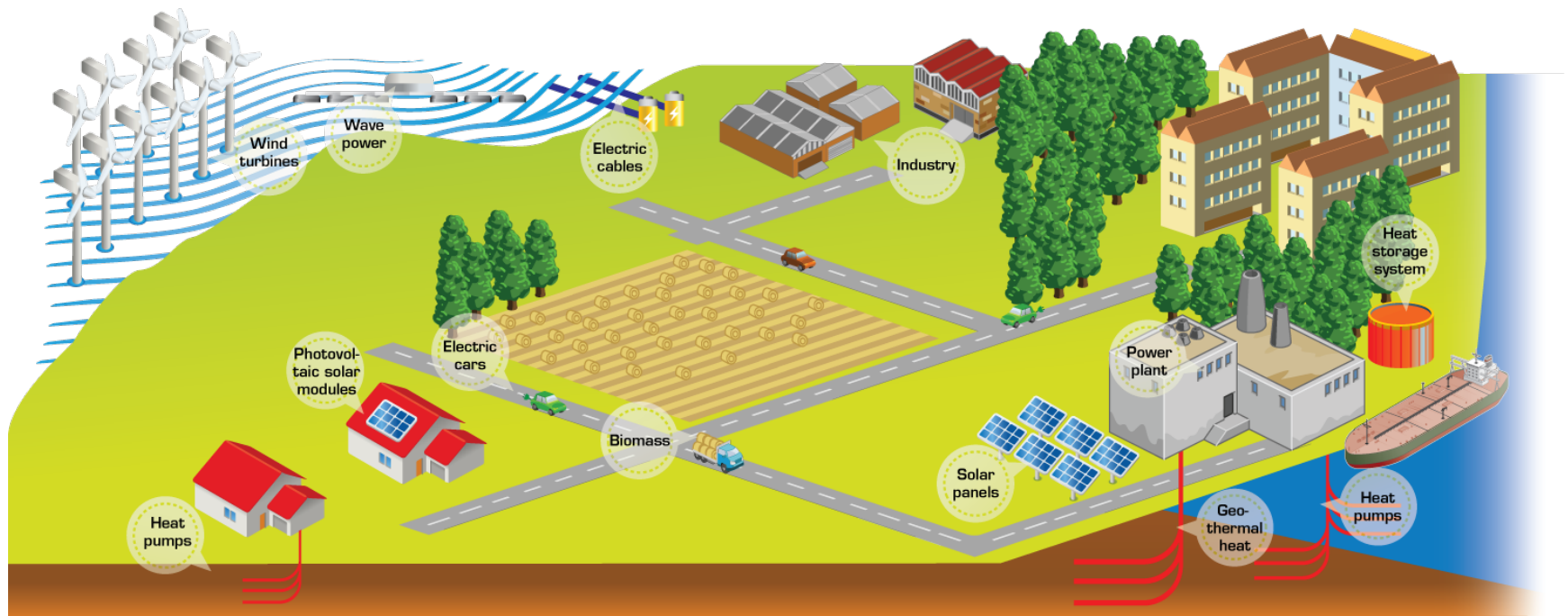
## Hierarchical Control Structure



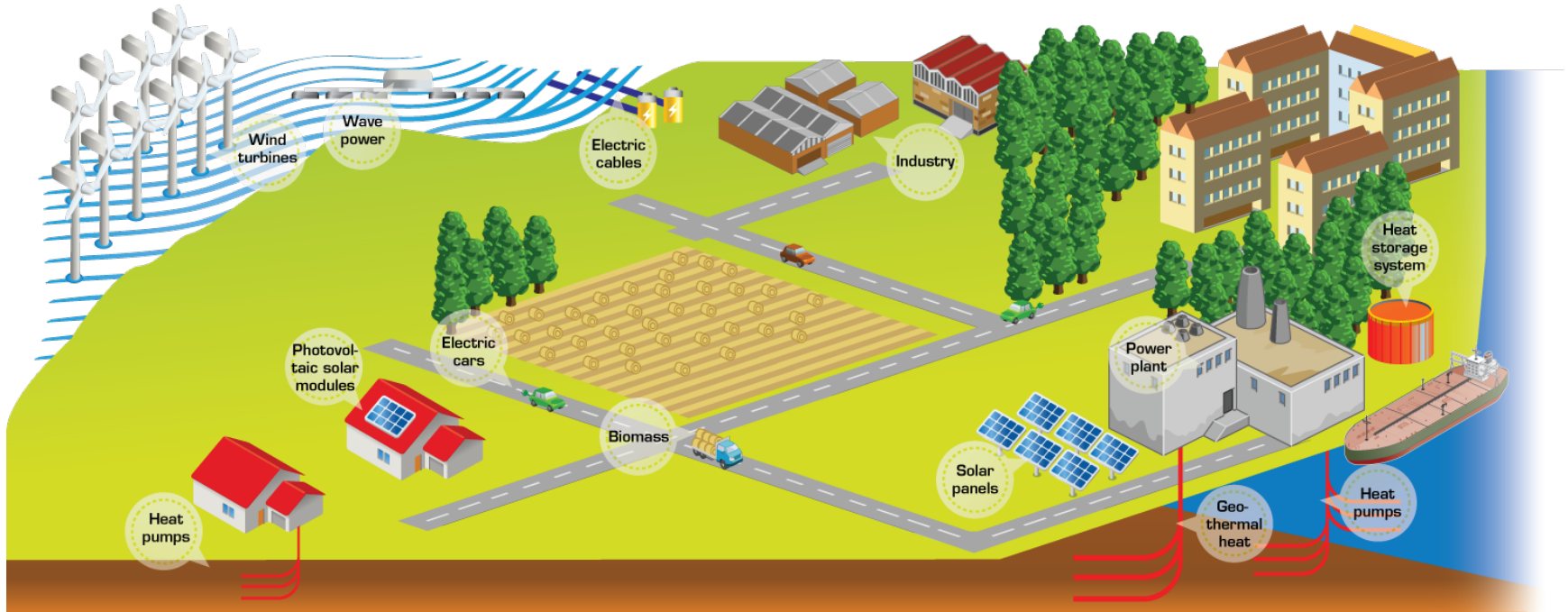
- Disturbances
- wind speed
  - ambient temp
  - solar radiation



# The Vision of Energy-Smart Cities



# Smart Energy Systems



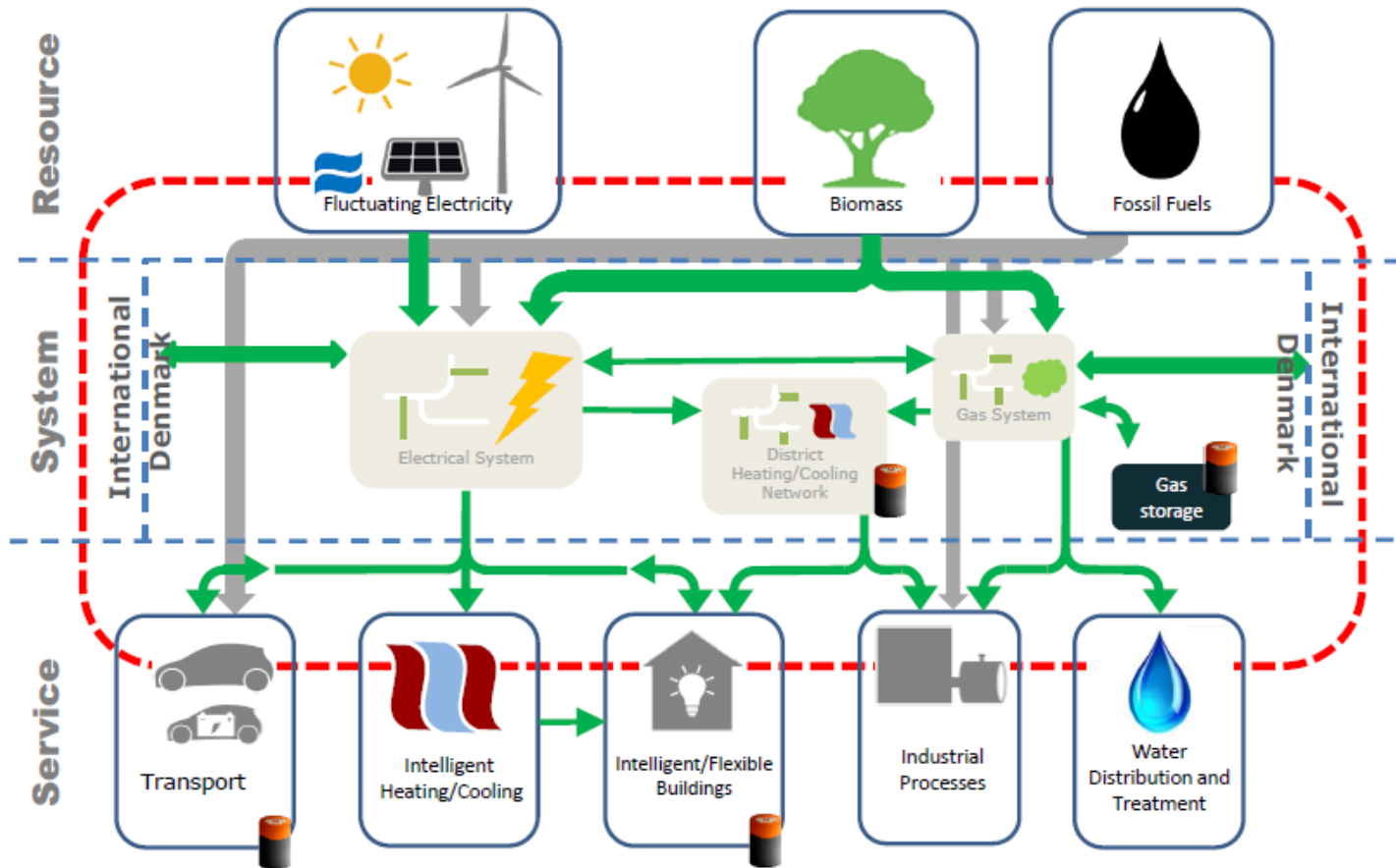
- **Thermal Storage**

- Heating of floors etc
- Heating of water accumulation tanks
- Refrigeration Systems

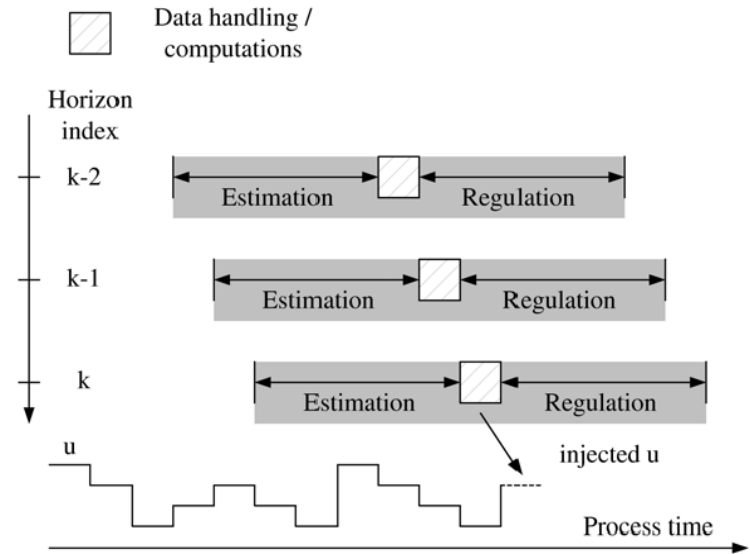
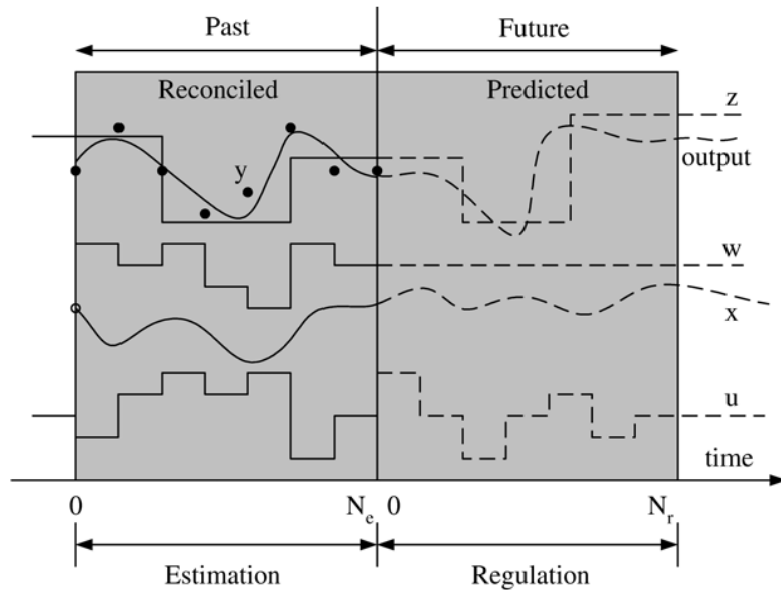
- **Power / Heat Producers**

- Wind Turbines
- Photovoltaic Solar Modules
- Solar Panels
- CHP Plants
- Fuel Cells

# Connected and Integrated Energy Systems - Model Predictive Control is the enabler



# Model Predictive Control

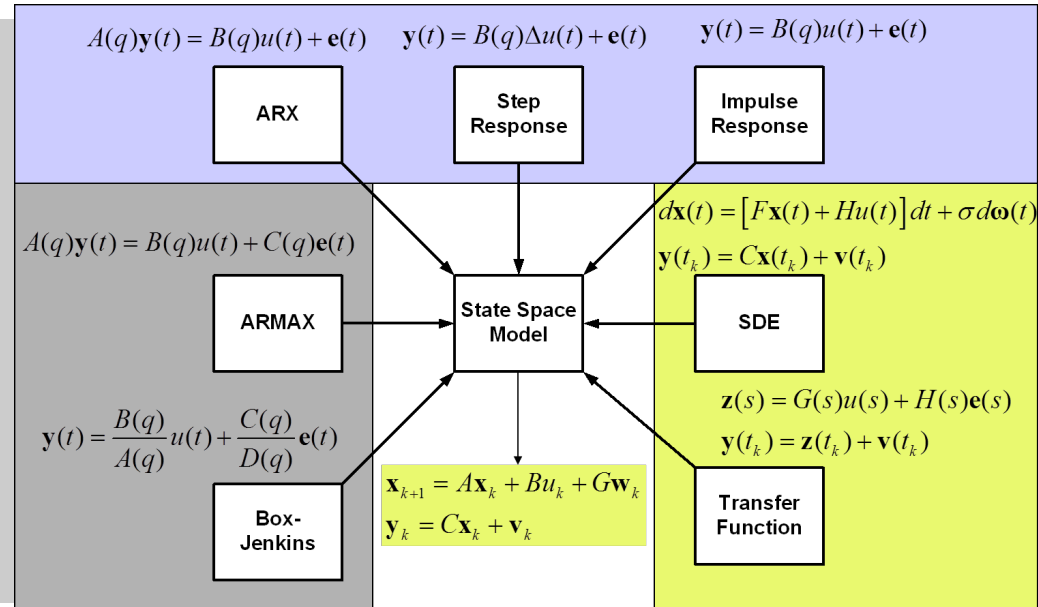
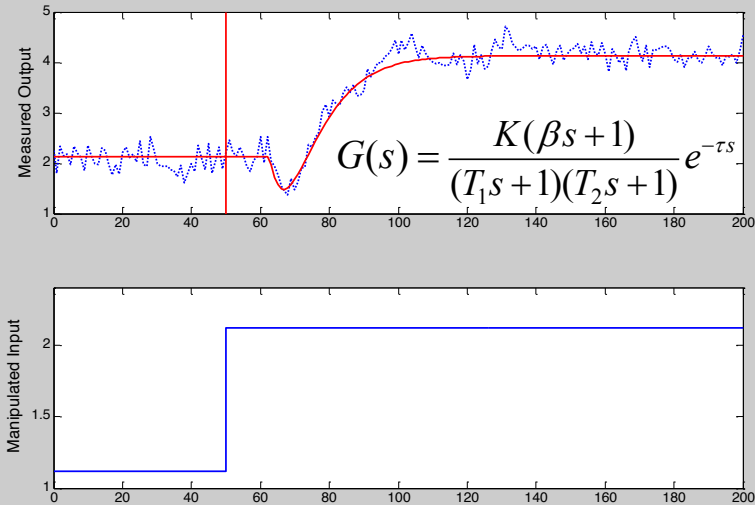


$$\min_{\{u_k, x_{k+1}\}_{k=0}^{N-1}} \phi = \phi(\{u_k, x_{k+1}\}_{k=0}^{N-1}; x_0, \theta)$$

$$s.t. \quad x_{k+1} = F_k(x_k, u_k, \theta) \quad k = 0, 1, \dots, N - 1$$

$$u_k \in \mathcal{U}$$

# Data based prediction models



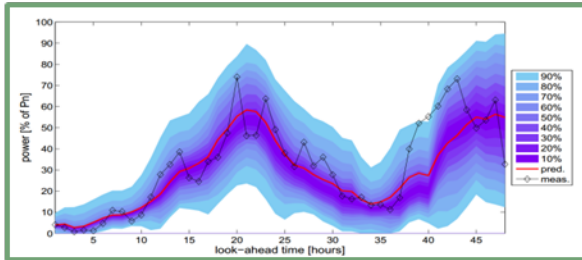
The models for filtering and prediction are

- Adaptive
- Data-based
- Combines a-priori (model) and a-posterior (data) information
- Able to predict the mean values and the uncertainties

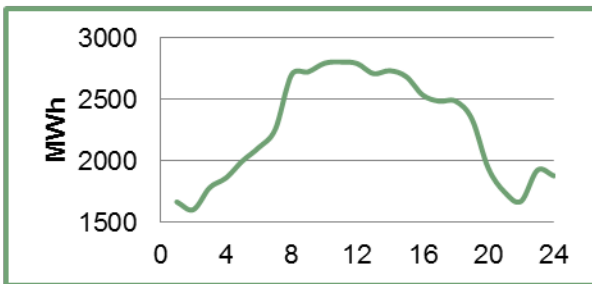


# Control of Energy-Smart Systems = Economic Model Predictive Control

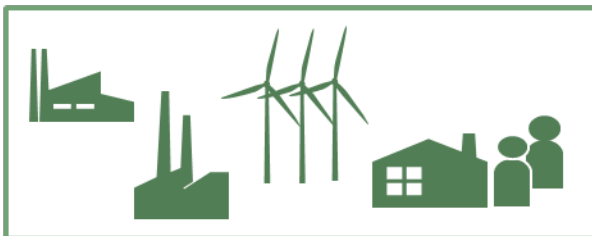
Wind Power Forecast



Consumption Forecast



Unit Specifications



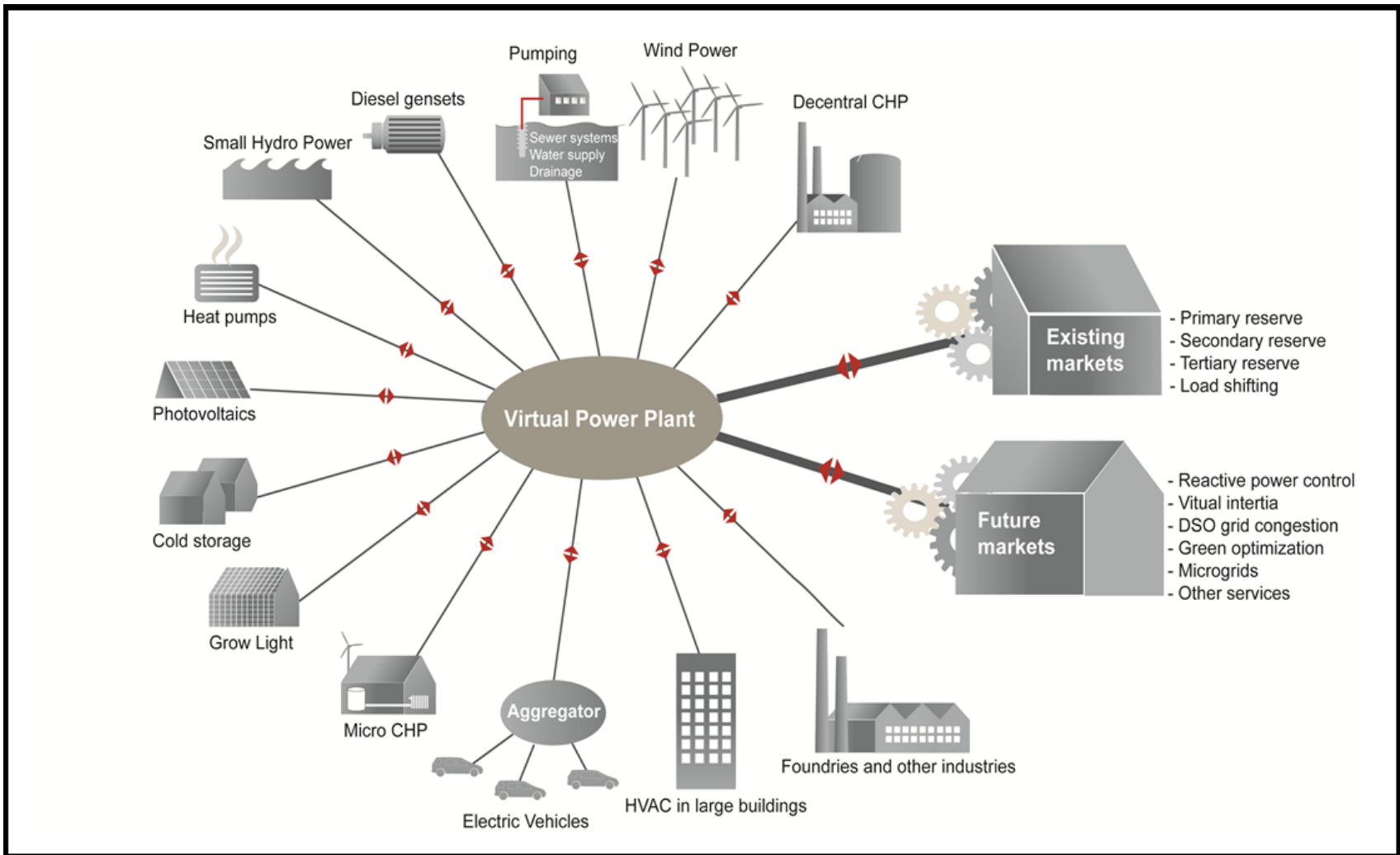
Planning Tool



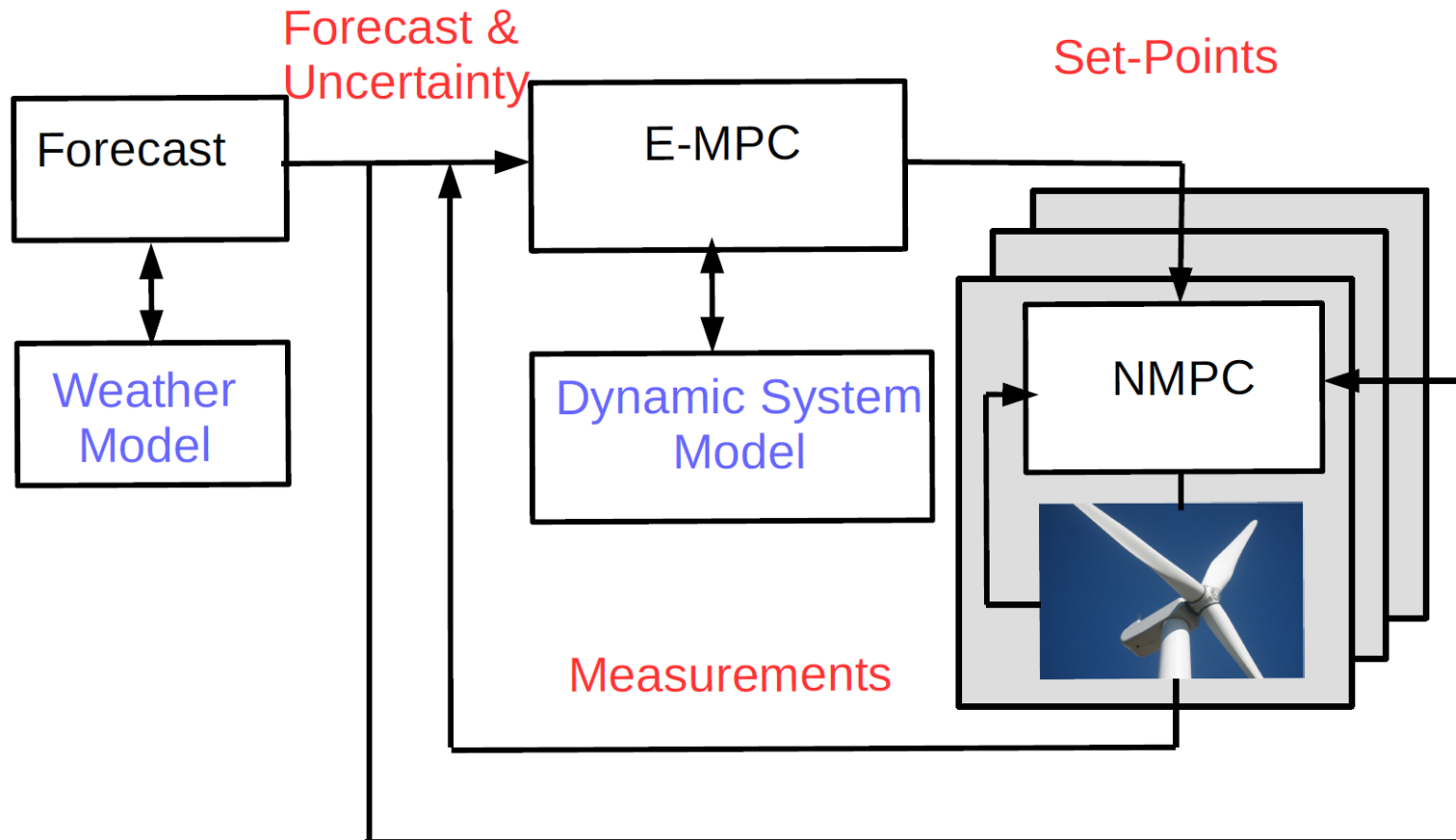
Plan



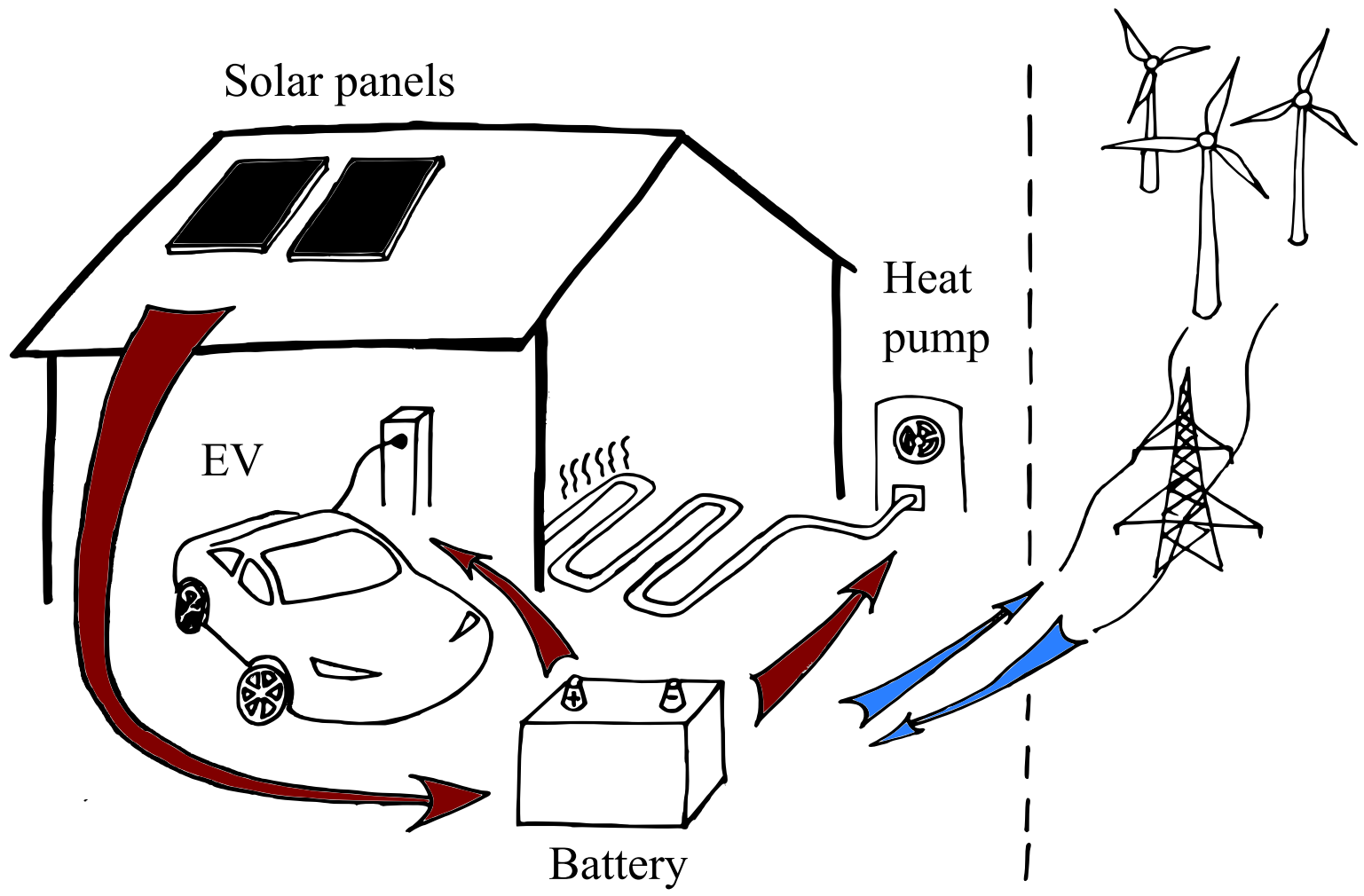
# Virtual Power Plant



# Forecast Based Hierarchical MPC



# The Vision of Energy-Smart Homes



# Elon Musk's vision of an energy-smart home





# Electric Vehicles

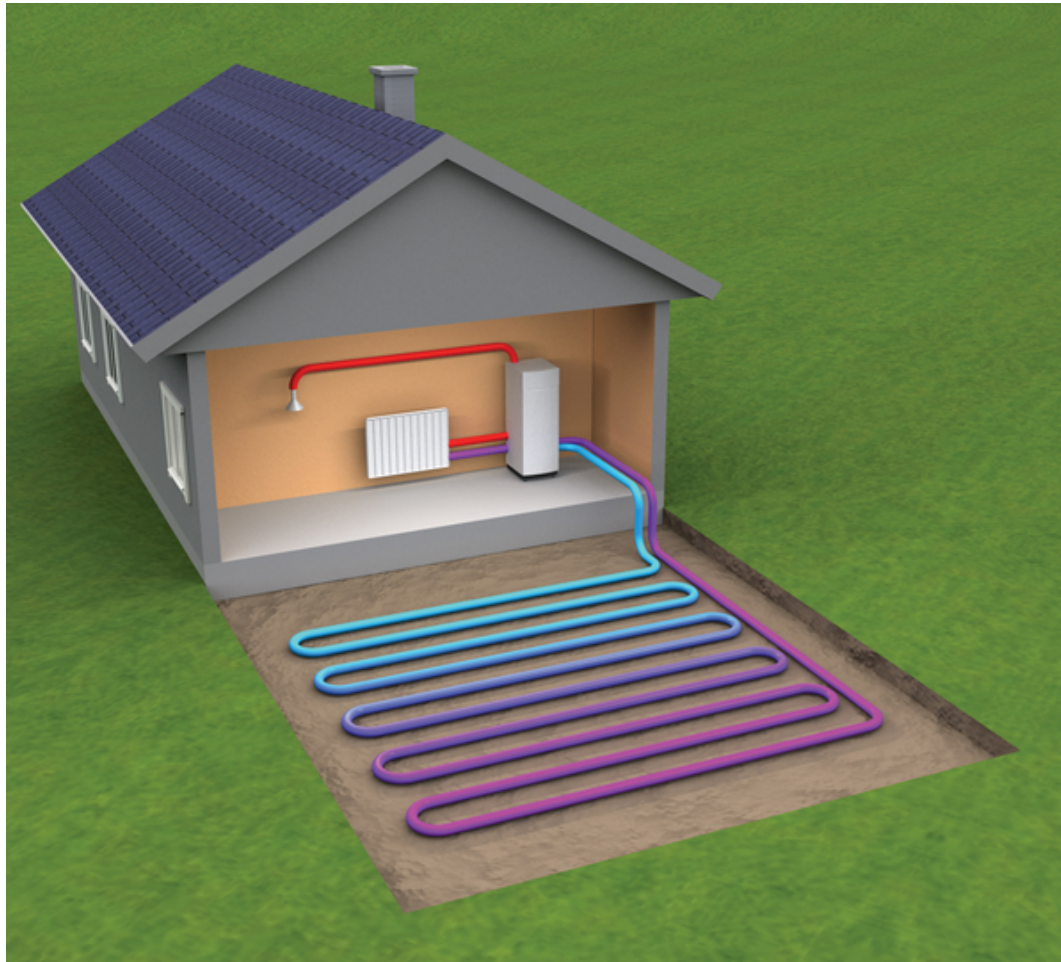




# Solar roof tiles



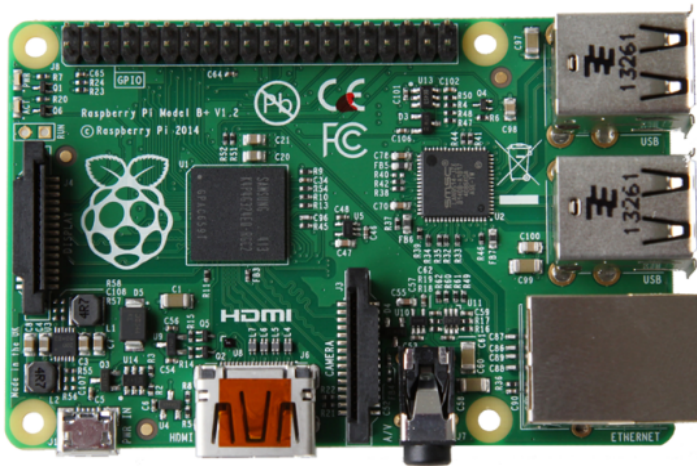
# Heat Pumps



# Smart Energy Consumption in a Residential Home

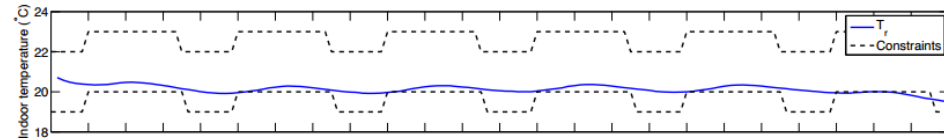
## Raspberry Pi Embedded Control

Embedded MPC Algorithms for control of individual energy units



## Control from the cloud

The control and forecasting systems are in the cloud.



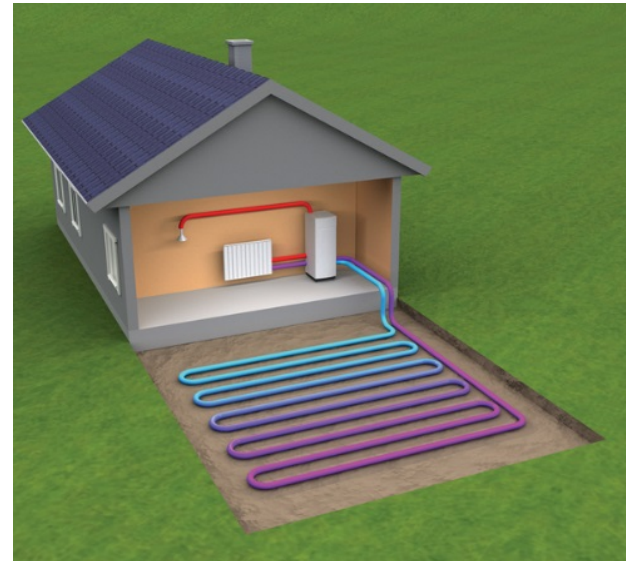
$$\min_{\{u_k, x_{k+1}\}_{k=0}^{N-1}} \phi = \sum_{k=0}^{N-1} l_k(x_k, u_k) + l_N(x_N) \quad (1a)$$

$$s.t. \quad x_{k+1} = A_k x_k + B_k u_k + b_k \quad k \in \mathcal{N} \quad (1b)$$

with  $\mathcal{N} = \{0, 1, \dots, N-1\}$  and stage costs defined by

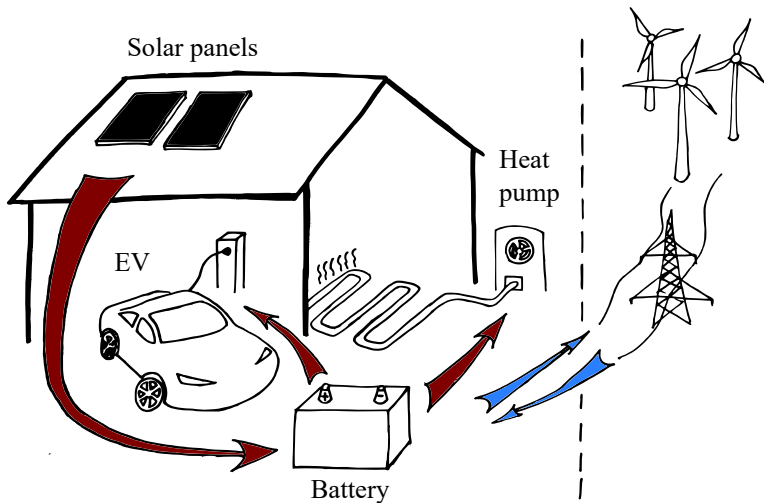
$$l_k(x_k, u_k) = \frac{1}{2} \begin{bmatrix} x_k \\ u_k \end{bmatrix}' \begin{bmatrix} Q_k & M_k' \\ M_k & R_k \end{bmatrix} \begin{bmatrix} x_k \\ u_k \end{bmatrix} + \begin{bmatrix} q_k \\ s_k \end{bmatrix}' \begin{bmatrix} x_k \\ u_k \end{bmatrix} + \rho_k \quad (2a)$$

$$l_N(x_N) = \frac{1}{2} x_N' P_N x_N + p_N' x_N + \gamma_N \quad (2b)$$





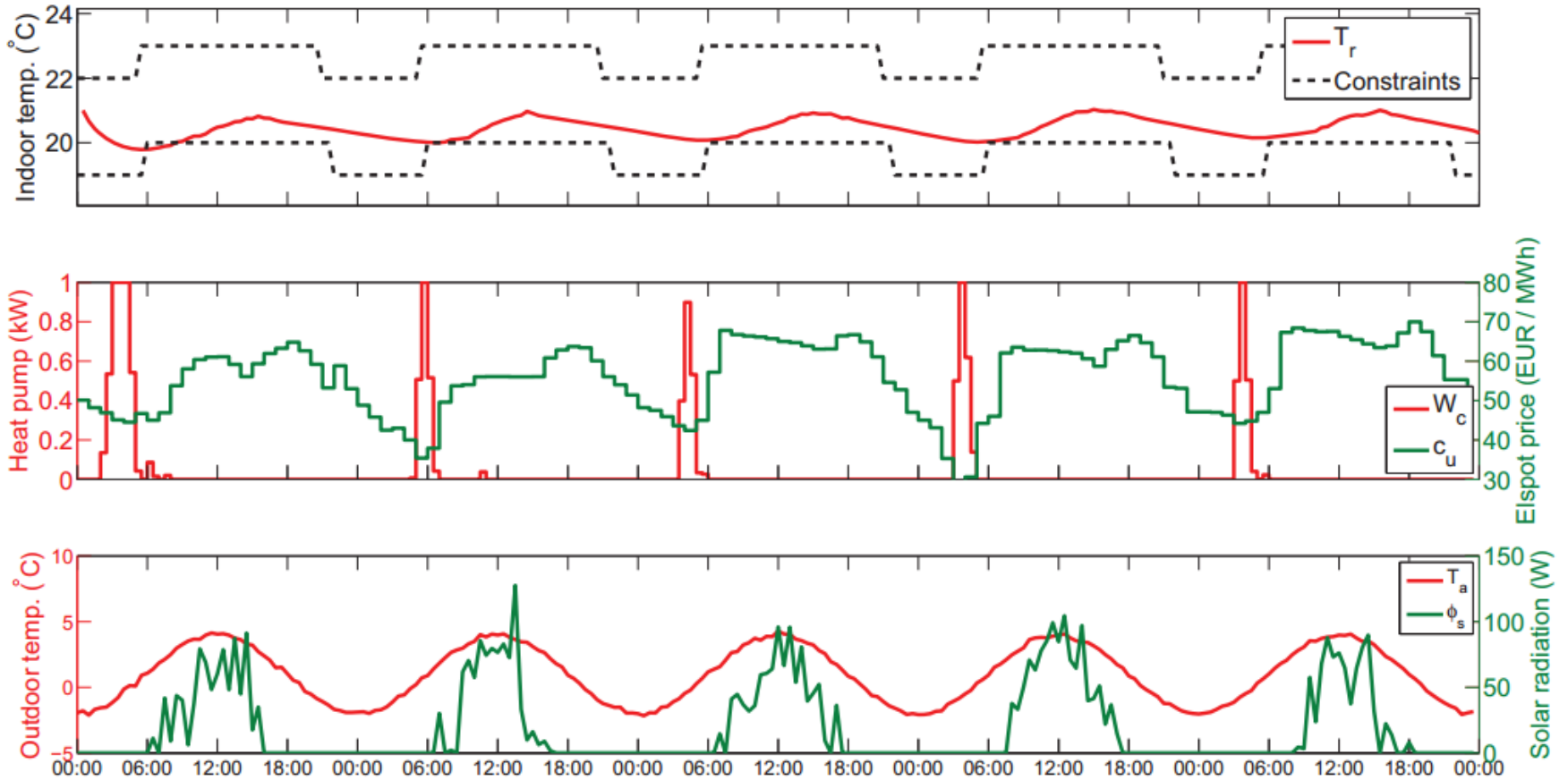
# Scientific advances in Economic MPC to enable smart energy homes



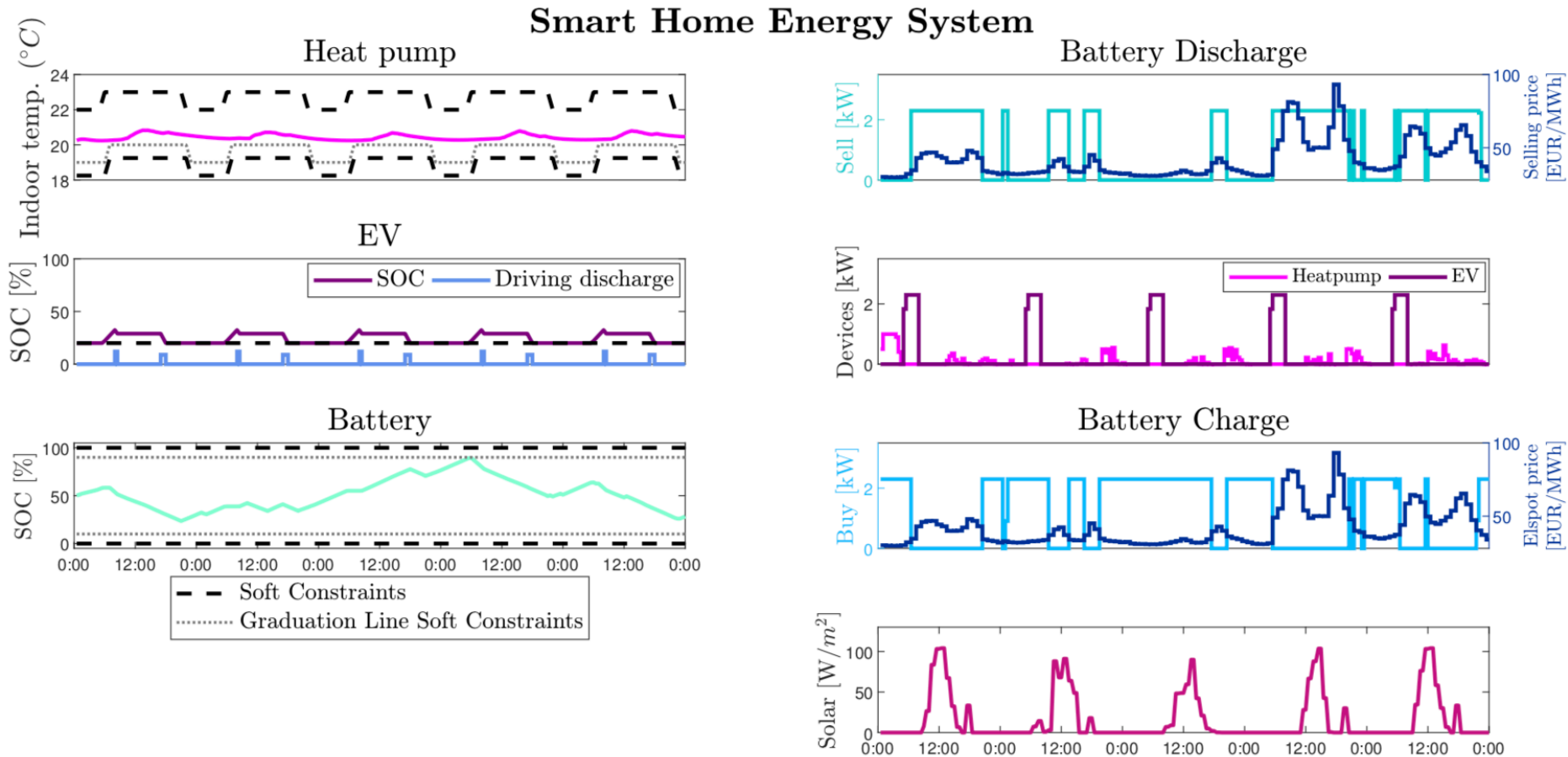
Economic MPC for Smart Energy Homes – a number of scientific advances

- Multi-level soft constraints
- Cost-to-go function – value of energy stored at the end of the prediction horizon
- A simple model for simulation, control and optimization of such systems
- Efficient algorithms and computational technologies

# Economic MPC for Building Climate Control

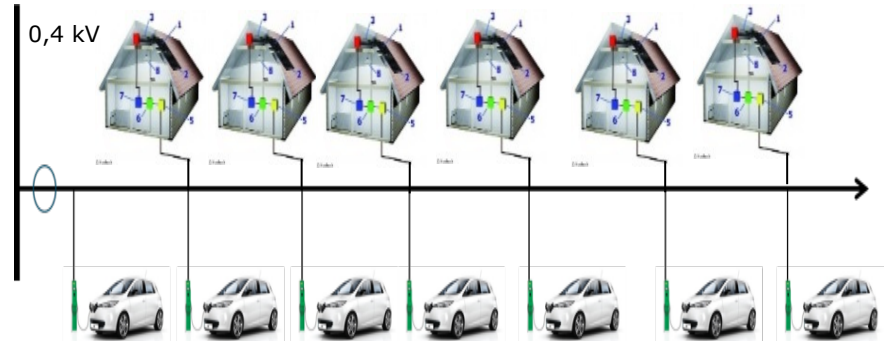


# Model Predictive Control for a Smart Energy Home – Simulation Results

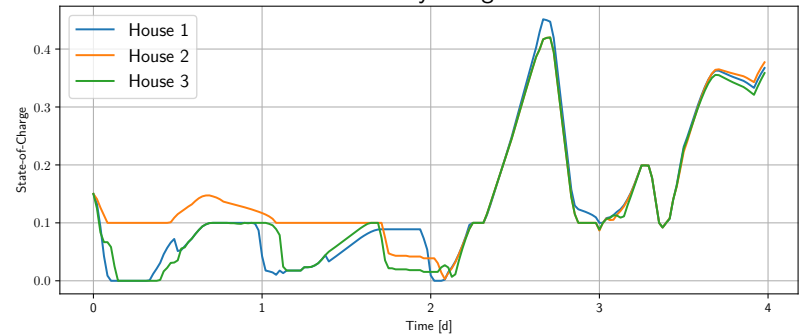




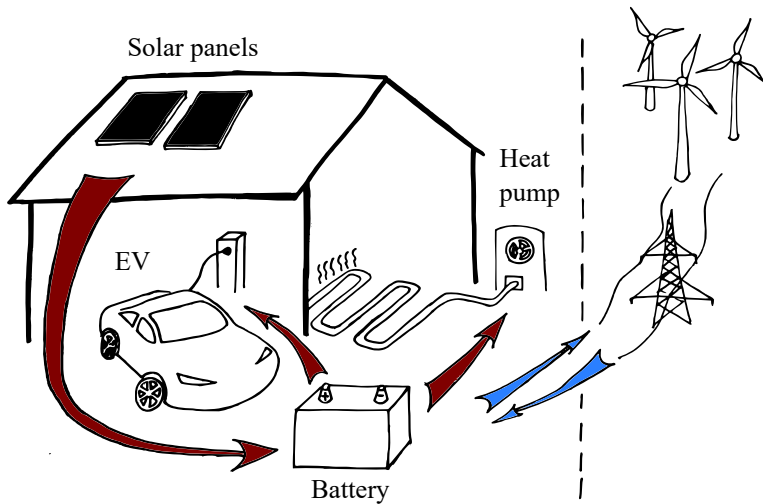
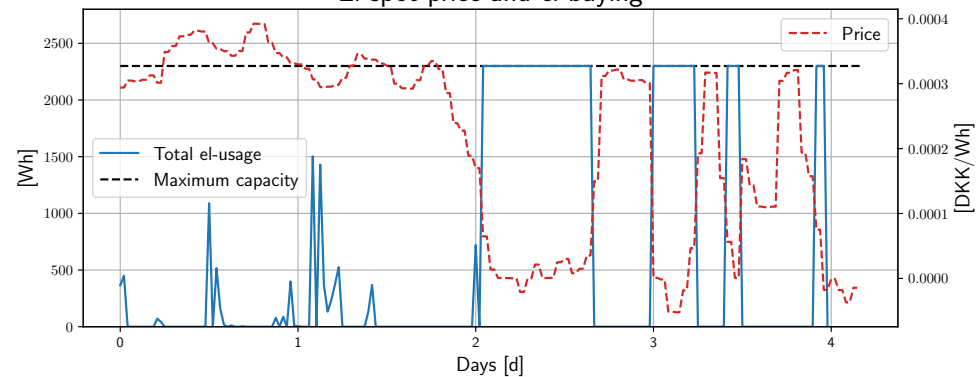
# A neighborhood of smart energy homes - Lærkevej



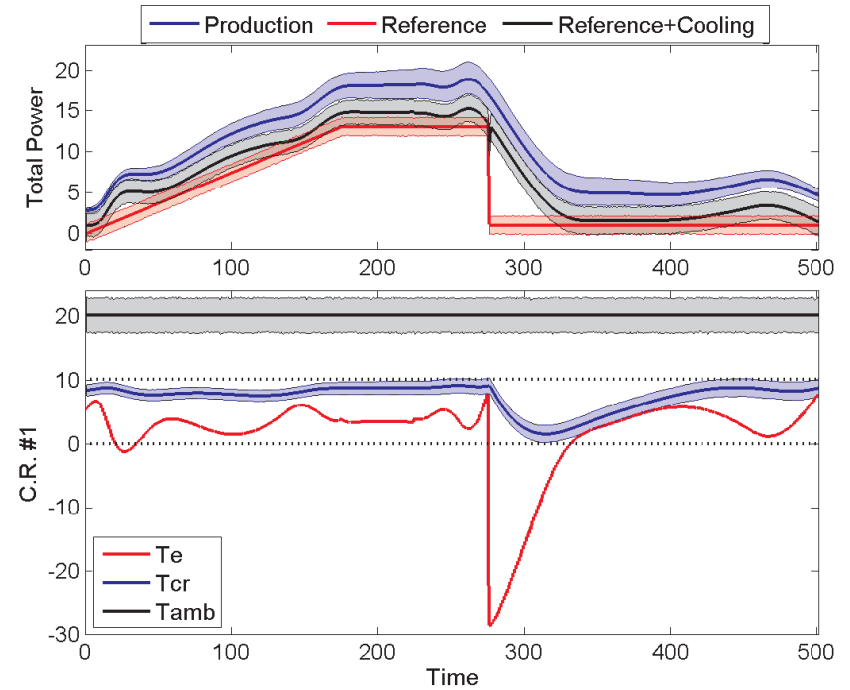
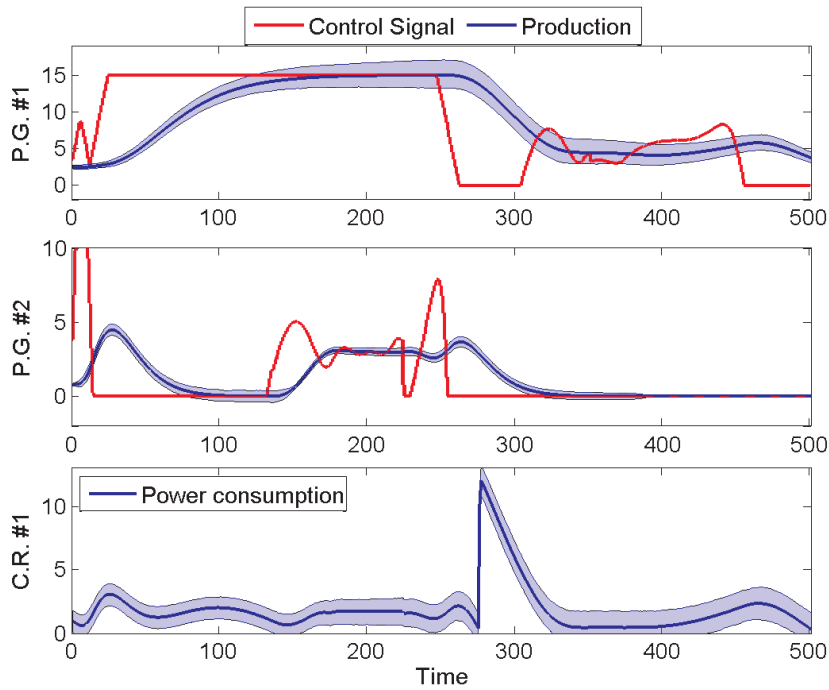
Battery charge



El-spot price and el-buying

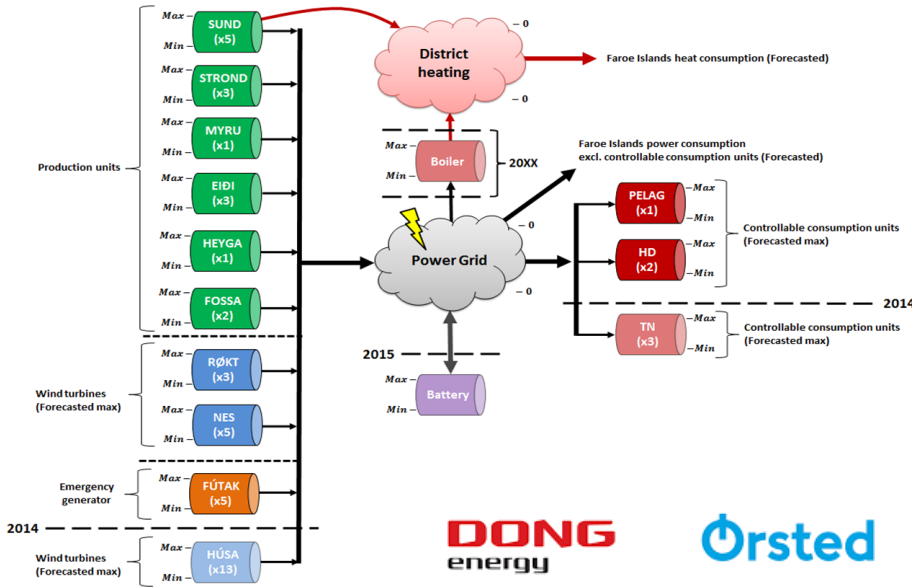


# Supermarket Refrigeration – Demand Response

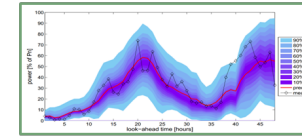




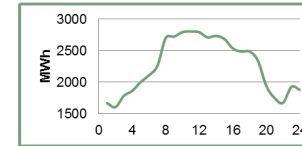
# The Faroe Island Power System



Wind Power Forecast



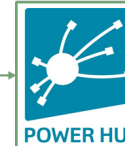
Consumption Forecast



Unit Specifications



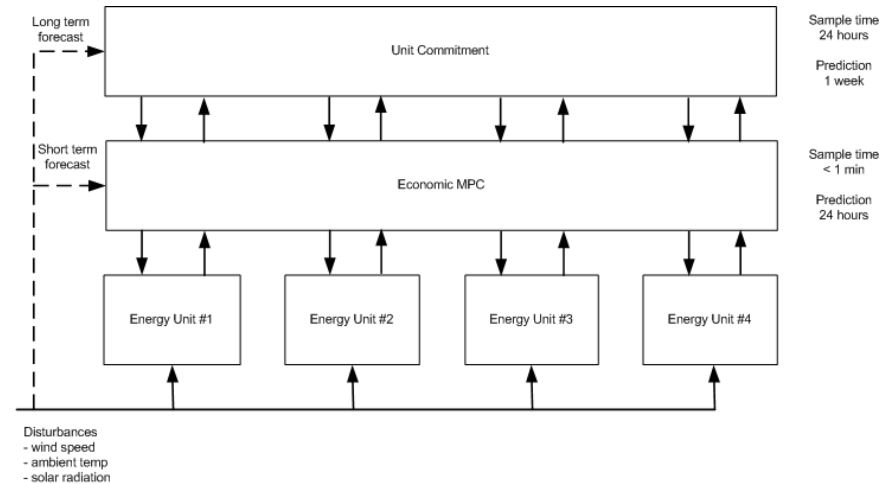
Planning Tool



Plan



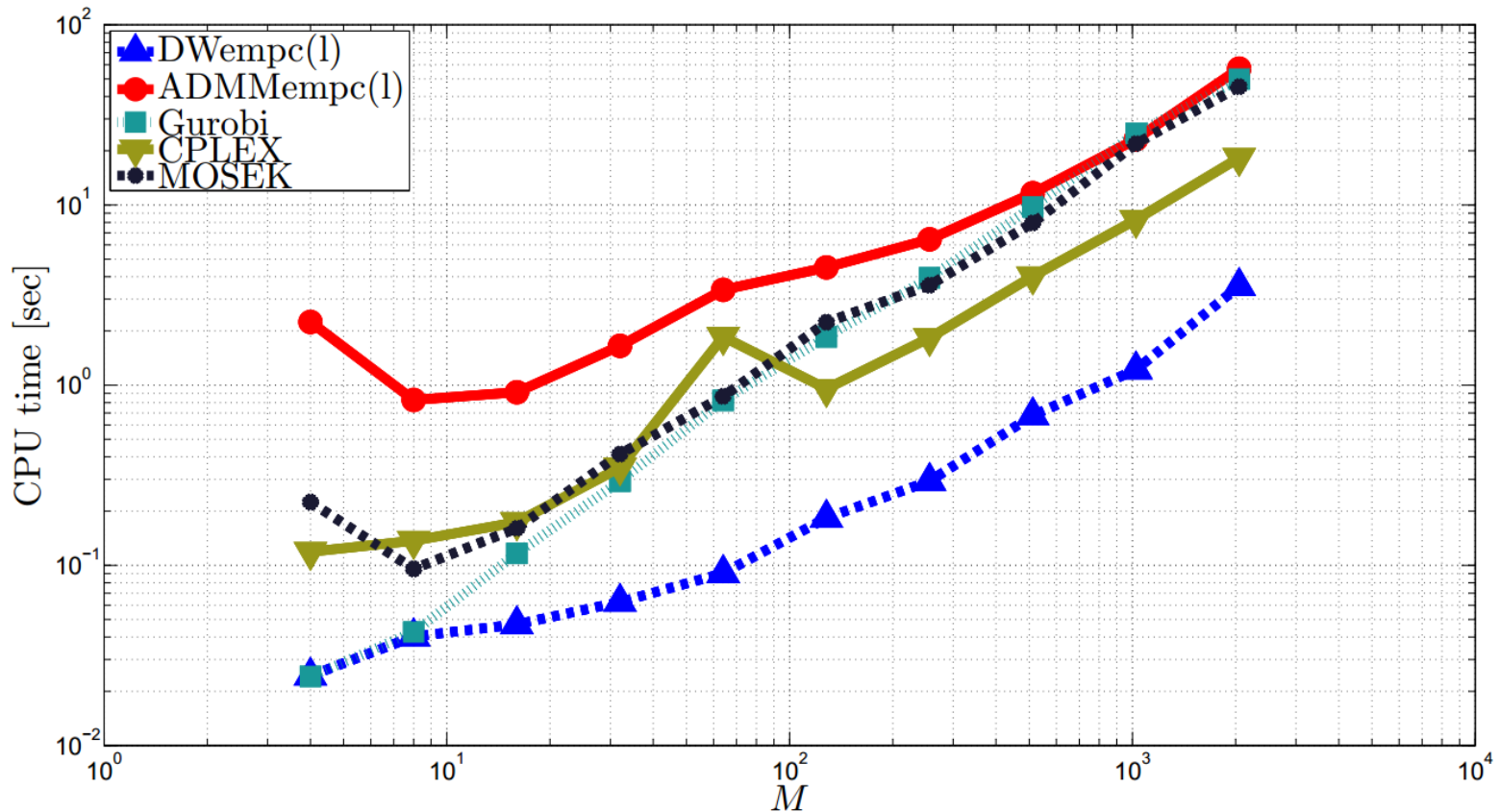
- Controlled the entire Faroe power system for 3 months
- Economic MPC system developed by Orsted (Dong Energy) and DTU Compute as part of an industrial PhD project



# Fast Solver for Direct Control of an Entire City

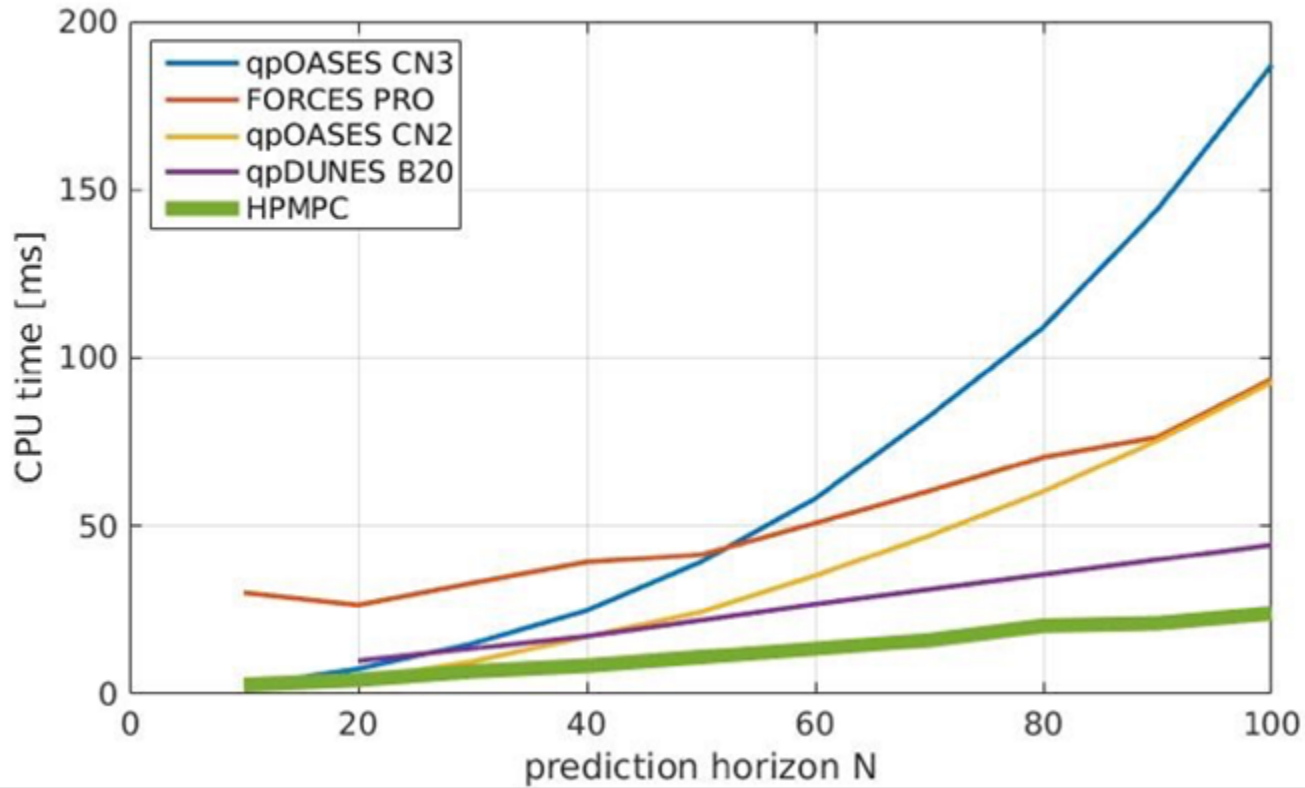
A Dantzig-Wolfe Decomposition Algorithm for  
Linear Economic Model Predictive Control of Dynamically Decoupled Subsystems

L.E. Sokoler<sup>a,b</sup>, L. Standardi<sup>a</sup>, K. Edlund<sup>b</sup>, N.K. Poulsen<sup>a</sup>, H. Madsen<sup>a</sup>, J.B. Jørgensen<sup>a,a</sup>



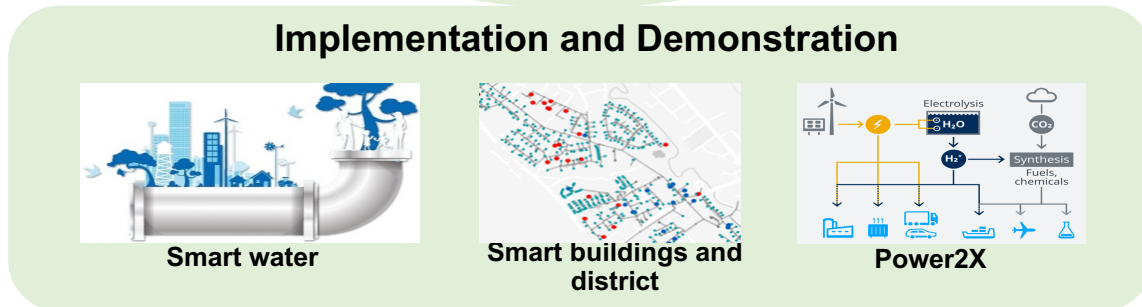
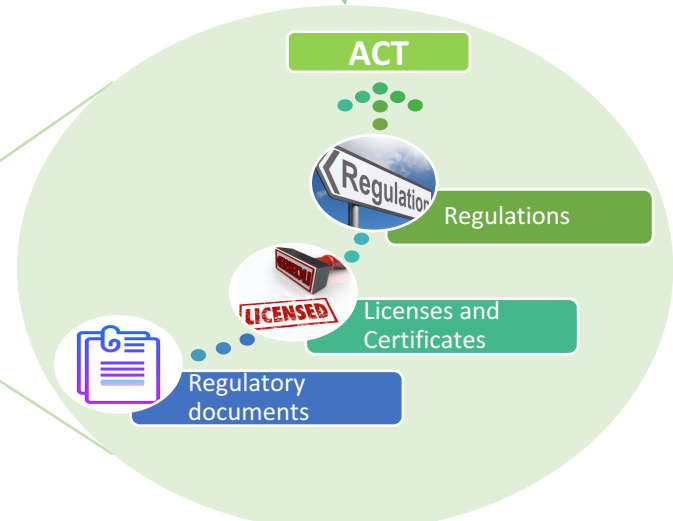
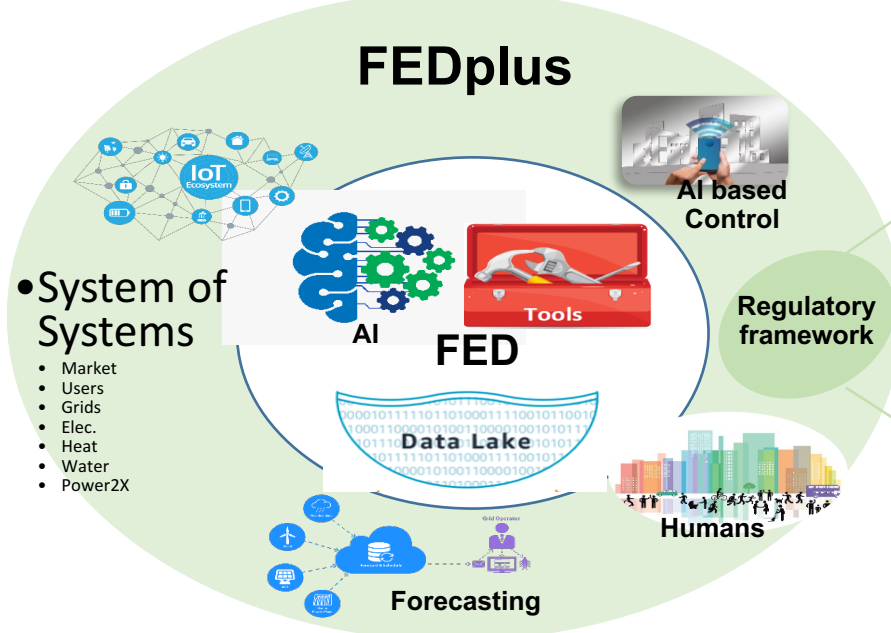
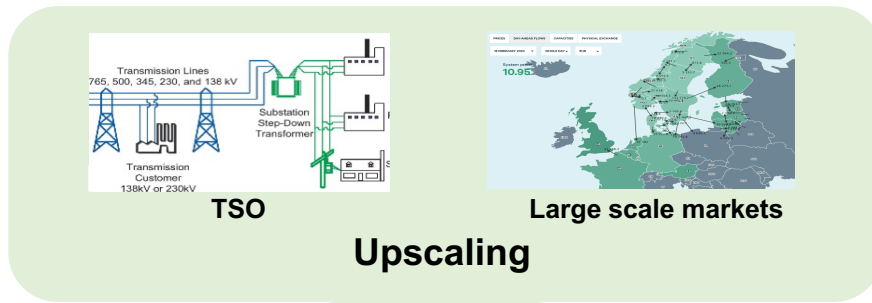


# Fast Algorithms for Model Predictive Control - enable new applications

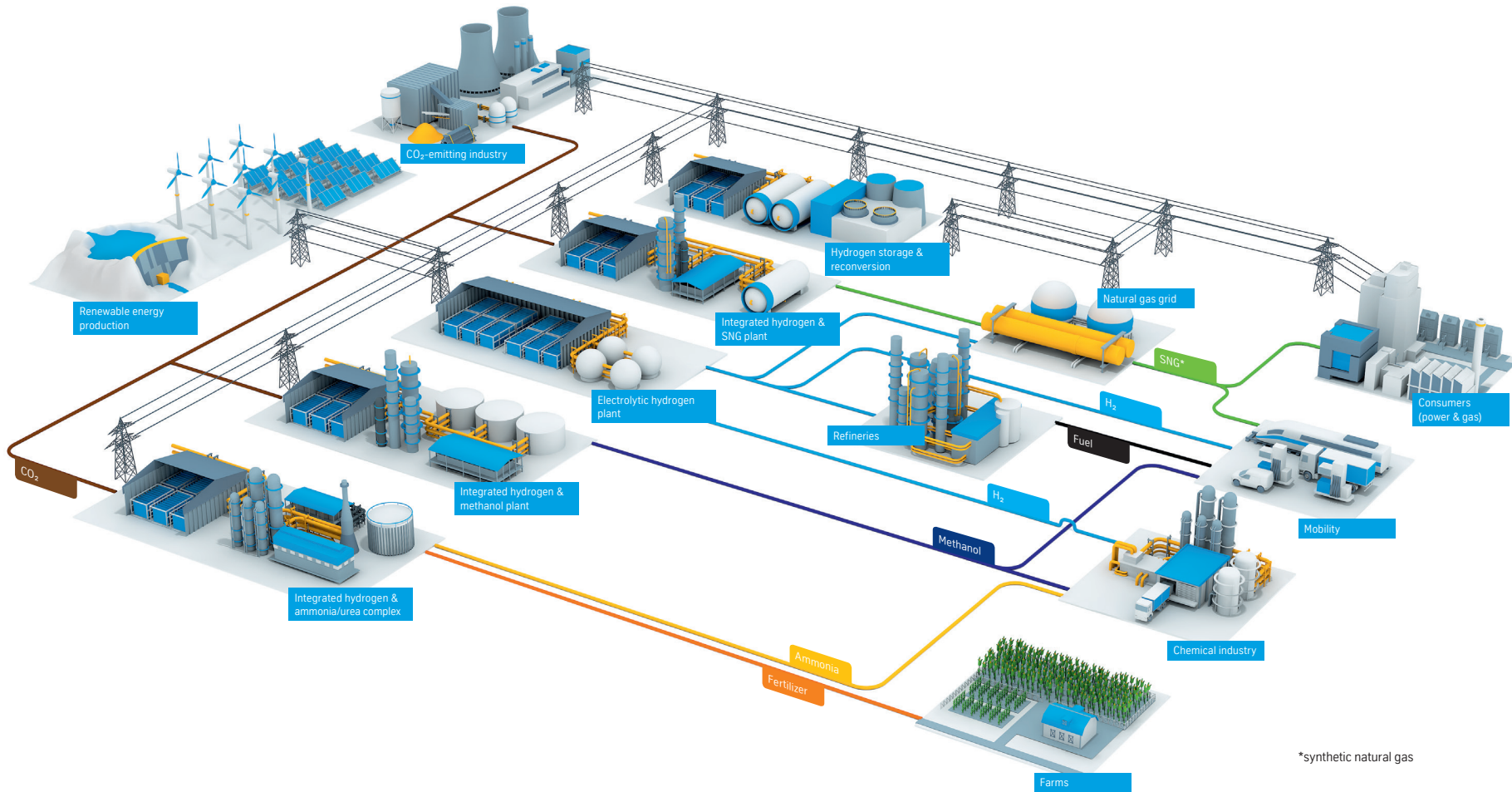




# FEDplus

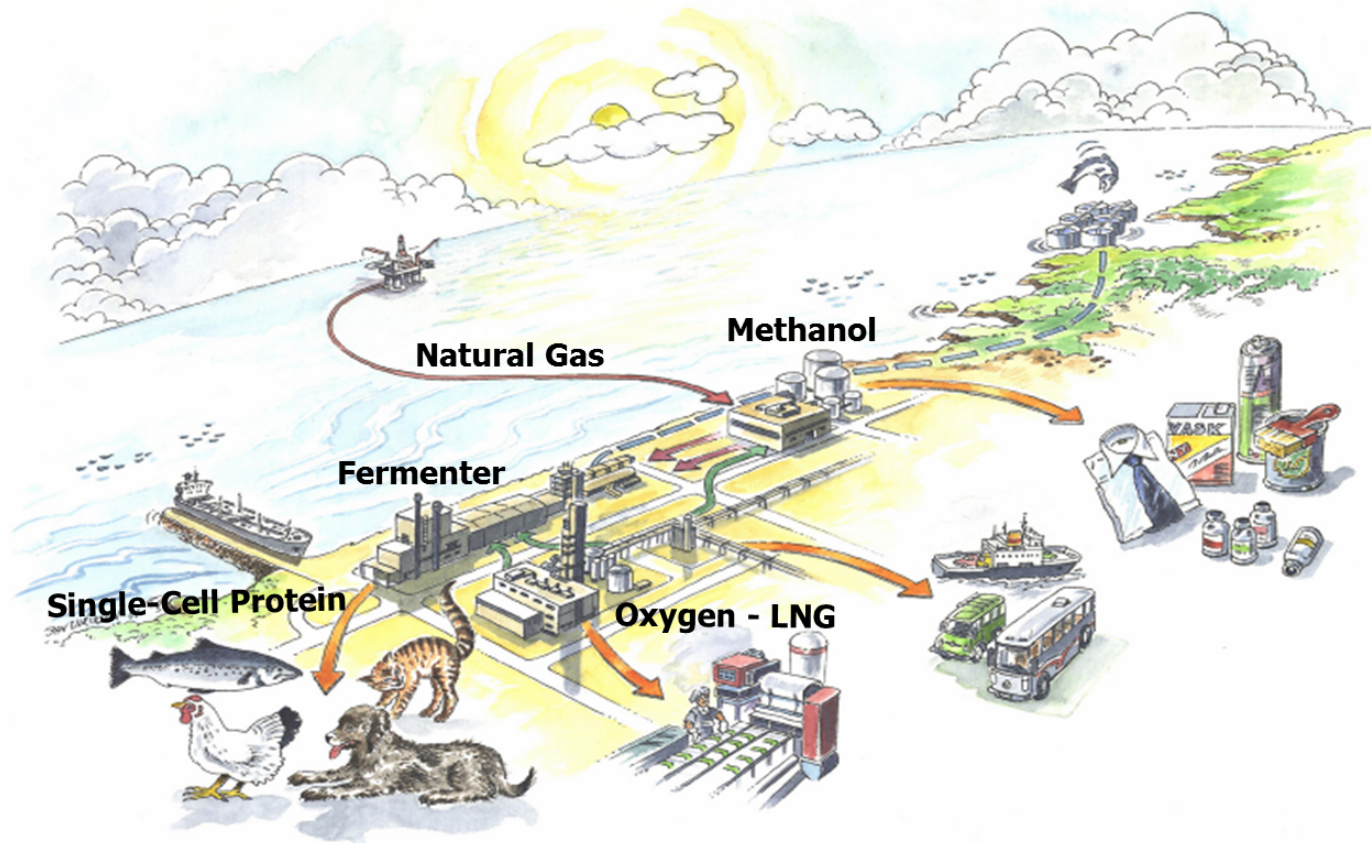


# Power-2-X



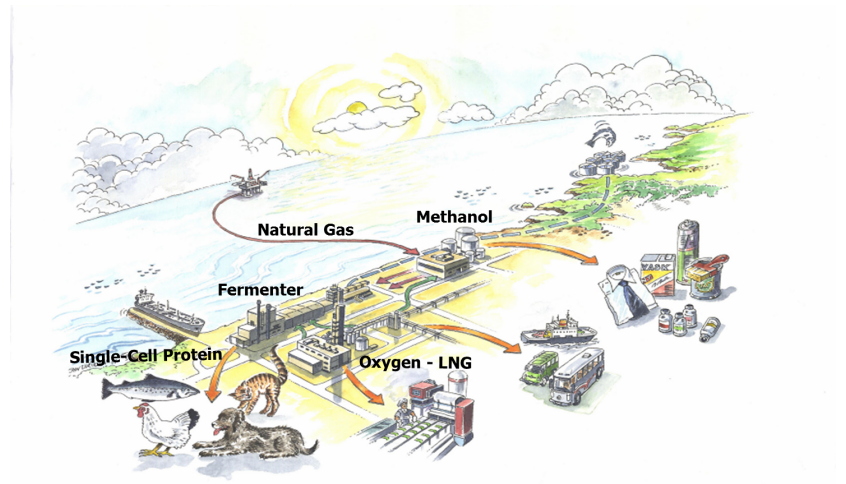
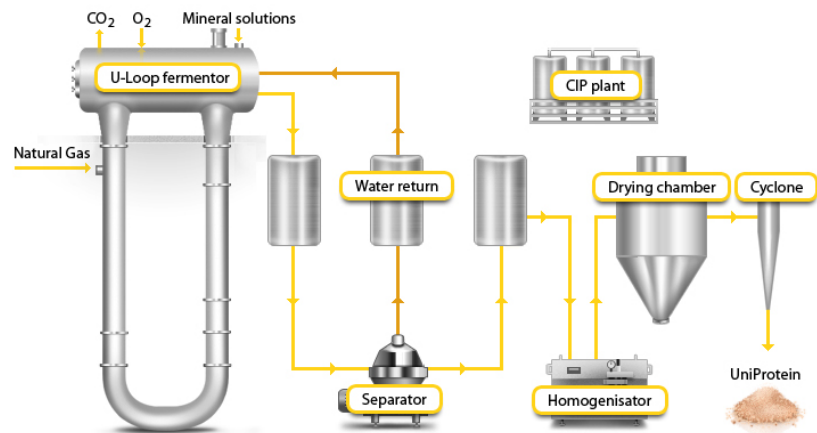
\*synthetic natural gas

# Proteins from methane - natural gas, biogas, SNG





# Single-Cell Protein

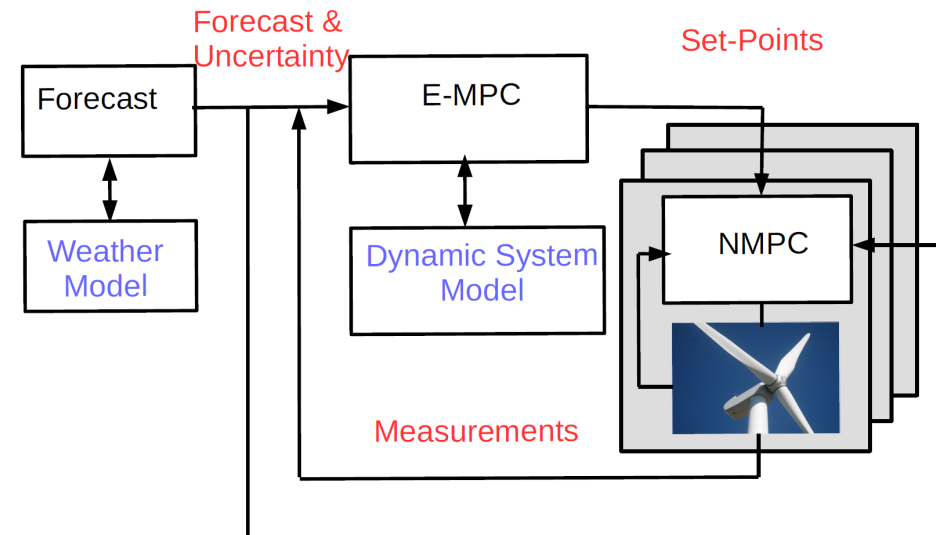
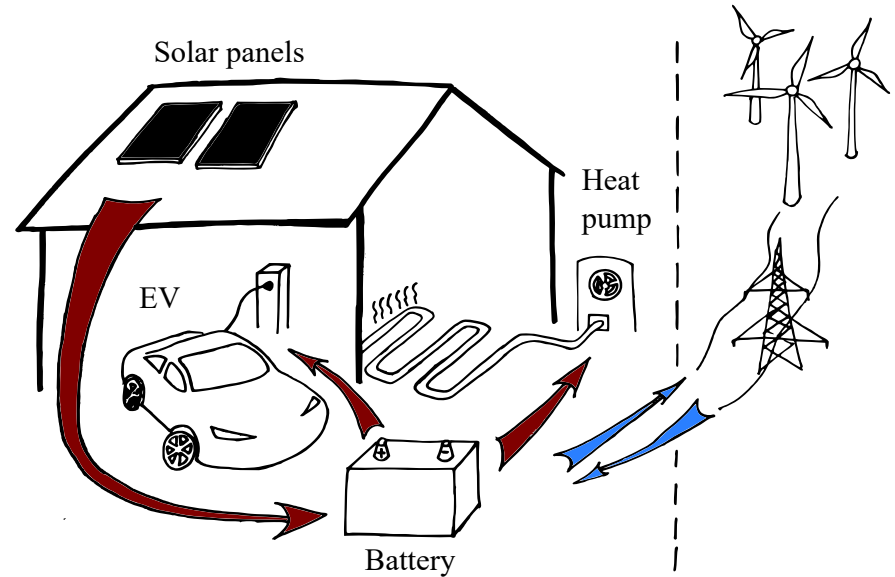






# Summary

- MPC technology implemented in many systems to enable coordinated and efficient operation
- Industrial energy related processes
  - Cement Processes (FLSmidth)
  - Food processes (GEA Process Engineering)
- Energy Processes
  - Energy system control (Orsted)
  - Wind turbine control (Vestas)
- MPC technology is mature and ready to be implemented on large scale for buildings to enable smart cities and smart energy homes.
- MPC technology is the key enabler for integrated and coordinated systems





# Thank You – Q&A



Smart Cities  
Accelerator



**John Bagterp Jørgensen**

Technical University of Denmark

E-mail: [jbjo@dtu.dk](mailto:jbjo@dtu.dk)

DTU Compute

Department of Applied Mathematics and Computer Science

